Modular Hadamard Matrices

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A Hadamard matrix is a square matrix H of order n, with coefficients ± 1 , satisfying the orthogonality condition $H \cdot H^{\top} = nI$. There are two classical conjectures about them:

• Hadamard's conjecture, according to which there should exist a Hadamard matrix of order n for every n divisible by 4.

• Ryser's conjecture, stating that there exists no *circulant* Hadamard matrix of size n for n > 4.

In this talk we will consider the somewhat weaker notion of *modular* Hadamard *matrices*. These are also square matrices of size n with coefficients ± 1 , but for which the above orthogonality condition is only required to hold modulo some fixed integer m.

We will discuss the above two problems in the modular context, and present some results obtained in joint work with M. Kervaire. These include a complete solution of the 32-modular analogue of Hadamard's conjecture, and the construction of intriguing families of circulant modular Hadamard matrices.